

Intensive Lectures on the Algebraic Montgomery-Yang Problem

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August 7–8, 2026

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Abstract

A normal projective surface with the same Betti numbers of the projective plane $\mathbb{CP}^2$ is called a rational homology projective plane or a $\mathbb{Q}$ -homology $\mathbb{CP}^2$. People working in algebraic geometry and topology have long studied a $\mathbb{Q}$ -homology $\mathbb{CP}^2$ with possibly quotient singularities. It is well-known that it has at most five such singular points, but it is still mysterious what is the optimal upper bound for the number of quotient singular points. This is the *algebraic Montgomery-Yang problem*, which is one of the most famous conjectures in this field.

Recently, we announced a complete resolution of the algebraic Montgomery-Yang problem. The goal of this intensive lectures is to give an overview on it, and then we explain briefly how to resolve it on the basis of main technical result (Theorem 1.3) and how to apply it to the remaining case $(2, 3, 5, n)$ (Theorem 1.4). A schedule of the lectures is following:

– Program –

August 7 (Fri)

10:30-12:00 Jongil Park (SNU) - Overview 및 Outline

14:00-15:30 Woohyeok Jo (SNU) - A Sketch of Proof of Theorem 1.3 (Sec. 3 & Sec. 5)

August 8 (Sat)

10:30-12:00 Kyungbae Park (KNU) - A Sketch of Proof of Theorem 1.4 (Section 6)

14:00-16:00 Jongil Park (SNU) & Kyungbae Park (KNU) - Q & A